PATENT SPECIFICATION



Date of Application and filing Complete Specification: June 22, 1951. No. 14887/51. ...

Application made in United States of America on June 23, 1950. Complete Specification Published: April 7, 1954.

Index at acceptance:—Classes 40(7), AE(3R: 4P3); and 40(8), U18(A4: B4B).

COMPLETE SPECIFICATION

Improvements in or relating to Refracting Media

WESTERN ELECTRIC COMPANY, INCORPORATED, of 195, Broadway, New York City, New York State, United States of America, a Corporation of the 5 State of New York, United States of America, do hereby declare the invention, for which we pray that a patent may be granted to us, and the method by which it is to be performed, to be par-10 ticularly described in and by the following statement:-

This invention relates to refracting devices for waves of various kinds, including electromagnetic and compressional, 15 and more particularly, in the case of electromagnetic waves, to devices employing artificial media possessing an effective permeability and to the combination of such media with artificial di-

20 electric media.

The fabrication and use of artificial dielectric media for electromagnetic waves has been described in our copending application Serial No. 664,672, in which conductive elements such as metallic spheres or discs are arranged in a threedimensional array analogous to the molecular lattice of a crystalline dielectric. There is an electric polarization en-gendered in such an array of elements by an electromagnetic wave, that is equivalent in many respects to the polarization of a natural dielectric

medium. 35 There are known to the art arrays of conductive elements which produce an effective permeability and may be characterized as constituting an artificial magnetic medium.

In accordance with the present invention artificial refractive media of various sorts are employed in making refracting devices for waves, elastic or electro-magnetic. In the electromagnetic case, combinations of artificial dielectric media with artificial magnetic media may be used to produce compound artificial refractive media in which boundary reflections are materially reduced or substantially prevented.

In particular, the use of artificial permeability in combination with an artificial dielectric yields a refractive medium having the same impedance as free space but having a lower velocity of propaga- 55 tion for electromagnetic waves. Because the impedances of free space and this compound refractive medium are the same, reflections at the surface are sub stantially eliminated.

In the case of compressional waves acoustic waves, elastic waves and the like rigid elements take the place of the conductive elements in the arrays and the resulting media are useful in the delay and refraction of the particular kind of waves for which the device is &-

signed.

A satisfactory theory of artificial refractive media may be based upon the 70 lumped element circuit equivalents of certain structures associated with hollow guides, pipe wave ${f from}$ which a generalization leads to the consideration of arrays of elements in free space.

In the accompanying drawings:

Fig. 1 is a perspective view of a section of hollow pipe wave guide with barrier plates defining a slot perpendicular to the direction of the electric vector, to-80 gether with a diagram native representa-tion of the equivalent lumped circuit element corresponding to the slot, namely a capacitance;

Fig. 2 is a similar representation 85 except that the slot is parallel to the electric vector and the equivalent dumped circuit element is a shunt inductance;

Fig. 3 is a perspective view of a section of hollow pipe wave guide having a 90 channel-like extension in one wall and a series inductance as the equivalent lumped circuit element;

Fig. 4 is a perspective view of a section of hollow pipe wave guide having barrier 95 plates arranged as in the lower part of

75

[Price 2/8]

Fig. 1 together with a plurality of channel-like extensions like that in Fig. ture is shown diagrammatically at the 3 and having an equivalent lumped circuit which is a low-pass filter;

Fig. 5 is a perspective view of a point beam antenna system comprising a plano-convex, circularly

strip lens;

Figs. 6, 7 and 8 are, respectively, top sectional, side and front views of the lens included in the system of Fig. 5;

Fig. 9 is a perspective view of a channel-like element useful in practising

the invention:

Fig. 10 is a perspective view of a section of hollow pipe wave guide containing a channel element like that of Fig. 9 embedded in a filling of dielectric material such as polystyrene foam:

Fig. 11 is a perspective view, partly in section, showing an array of channels

in a frame;

Fig. 12 is a perspective view of a V-shaped element useful as an alternative 25 to the channel-like element of Fig. 9;

Fig. 13 is a perspective view of a a convex lens constructed of Vped elements as shown in Fig. 12 bedded in discs of dielectric material zich as polystyrene foam.

Fig. 14 is a perspective view of a lens similar to that of Fig. 13 but embodying strip elements as shown in Fig. 5 in addition to V-shaped elements as shown

35 in Fig. 13;
Fig. 15 is a perspective view of a double concave refracting structure employing wave guides somewhat like that shown in Fig. 3, operated in a mode of transmission in which waves accelerated rather than delayed and hence providing a structure which converges or focusses waves passing therethrough;

Fig. 16 is a view of the structure of Fig. 15 as sectioned upon a medial hori-

zontal plane.

Referring to Eig. 1, there is shown a section of rectangular hollow dielectric wave guide 20 with the longer dimension of the rectangular section shown horizontal. It is assumed that an electromagnetic wave to be propagated through the guide has its electric vector E oriented vertically as shown in the

figure. Upper and lower barrier plates 22 and 23 respectively having conductive surfaces are shown defining a slot 24, which has its principal direction perpen-

60 dicular both to the direction of the vector E and to the longitudinal axis of the guide. A slot oriented like the slot 24 is known to function in the guide like a shunt capacitance in a conventional 65 transmission line, and the lumped

element circuit equivalent of the strucright in the figure by a shunt condenser 24 in a conventional line; 25. Thus, a metallic constriction or iris in a hollow 70 pipe dielectric wave guide, oriented as in symmetrical, Fig. 1, is the equivalent in many respects of a capacitive shunt in a two-wire transmission line.

Fig. 2 shows a metallic constriction or 75 iris oriented at right angles to that in Fig. 1 with reference to the vector E. This arrangement is known to be equivalent to a shunt inductance in a two-wire line, as indicated diagrammatically at 80

the right in the figure.

Fig. 3 shows a channel-like cavity structure 26 in the top wall of a rectangular wave guide 27, the channel having a depth in the direction of the 85 electric vector somewhat less than a quarter wavelength at the desired operating frequency. This arrangement is known to produce the equivalent of a series inductance in a conventional trans-

mission line.

Fig. 4 shows a rectangular wave guide 28 in which a plurality of cavity structures 29 similar to the structure 26 in Fig. 3 are provided together with 95 a plurality of shunt capacitive structures 30 similar to the lower barrier plate 23 in Fig. 1. The structure of Fig. 4 is found to have as its lumped element circuit equivalent the circuit shown at the right 100 in the figure, the series inductances 31 corresponding to the channel-like cavity structures 29 and the shunt capacitances 33 corresponding to the constrictions formed by the barrier plates 30. The 105 structure of Fig. 4 is thus equivalent to loaded transmission line having series inductances and shunt capacitances, i.e., a low-pass filter. Such a line can readily be designed to have its 110 characteristic impedance equal to the characteristic impedance of the unloaded line and therefore can be connected into an unloaded line of the same construction without material impedance mis- 115 match. Moreover, because of the presence, of the series and shunt elements in the loaded section, the velocity of wave propagation in that section can be made materially smaller than that of the un-120 loaded line.

More particularly, the shunt capacitance per unit length in the loaded section may be adjusted to compensate, in its effect upon the characteristic im- 125 pedance, for the series inductance per unit length, while not compensating in its effect upon the velocity of propagation, analogously with lumped constant circuit theory. Thus, if Lo is the series 130 inductance per unit length and Co the shunt capacitance per unit length in the unloaded line, and L₁ and C₁, respectively, are the added series inductance and added shunt capacitance per unit length in the loaded section, the characteristic impedance Zo of the unloaded line is

$$Z_{Q} = \sqrt{\frac{L}{c_{o}}}$$
 (1)

10 while the characteristic impedance Z₁ of the loaded section is

$$Z_1 = \sqrt{\frac{L_0 + L_1}{c_0 + c_1}}$$
 (2)

By so proportioning L, and C, that

$$\frac{L_{o}}{C_{o}} = \frac{L_{o} + L_{1}}{C_{o} + C_{1}}$$
 (3)

15 it is seen that

$$Z_1 = Z_0 \tag{4}$$

when

$$\frac{L_1}{C_1} = \frac{L_0}{C_0} = Z_0^2$$
 (5)

The velocity of propagation vo for the 20 unloaded line on the other hand is

$$\dot{\mathbf{v}}_{\mathbf{o}} = \frac{1}{\sqrt{\mathbf{L}_{\mathbf{o}}\mathbf{C}_{\mathbf{o}}}} \tag{6}$$

while the velocity v₁ for the loaded section is

$$v_1 = \frac{1}{\sqrt{(L_o + L_1) (C_o + C_1)}}$$
 (7)

25 By comparison of equations (6) and (7) it is seen by inspection that positive values of L₁ and C₁ result in

$$v_1 < v_0^{-1}$$
 ... (8

that is, the velocity of propagation in the 30 loaded section is less than that in the unloaded line.

It should be noted that at higher frequencies, other modes of transmission, not possible at lower frequencies, occur as and the velocity of propagation for such

modes may be greater than the velocity of propagation in the unloaded line.

Image formation in the top, bottom and side walls of the guide 28 in Fig. 4 transforms the loaded guide into the 40 equivalent of a refractive medium of infinite extent consisting of arrays of channel-like cavity structures combined with arrays of conductive barrier strips. When the inductances and capacitances are 45 proportioned as specified by equation (3), the resulting medium is refractive to electromagnetic waves and at the same time introduces no reflection loss at the boundary between the unloaded medium 50. and the loaded medium. In other words, since the wave impedance of the loaded medium is equal to the wave impedance of the unloaded medium (or free space), there is no reflection loss to a wave pass- 55 ing across the boundary between the two media. The propagation velocity in the loaded medium however, is different from that in free space, so that lenses, prisms, etc., may be constructed from the loaded 60% medium which are capable of focussing, diffusing or otherwise refracting electromagnetic waves of suitable wavelength, with substantially no attendant reflec-

The right-hand portion of Fig. 4 indicates diagrammatically the impedances of the loaded and unloaded line and the velocity of propagation in each.

Figs. 5, 6, 7 and 8, show a lens structure employing capacitive elements alone without combining inductive elements, as disclosed in our copending Application Serial No. 664,673. This structure is repeated here to illustrate one type off capacitive medium which may be modified in accordance with the present invention to produce a non-reflective refracting structure.

Referring to Figs. 5, 6, 7 and 8, 80 reference numeral 70 denotes a unipolarized, circularly symmetrical, metallic delay lens comprising an array 71 of forty-nine conductive strip members 3 spaced apart a distance S₂ along the Y dimension, and a distance S₂ along the Z dimension, of a polystyrene foam medium 32. The forty-nine strips 3 are arranged in seven vertical panels 72 to 78 or, stated differently, in eight horizontal tiers 79 to 86. The foam medium 32 comprises eight vertically stacked slabs 87 to 94 which contain verticals slots, for retaining the strips 3 and support, wespectively, the eight whiers 79 to 86. The pectively, the front plane, the back convex face, the optical axis and the point focus of the lens 70. As shown on the

drawing the lengths of the slots and the strips 3, and the depths of certain outer slots and the \mathbf{widths} corresponding outer strips, are selected so as to conform to the vex contour of the back face 96 of the lens. Accordingly, while the number N of strips per unit area of the YZ section is constant throughout the array 71, the 10 array includes fractional, as well as whole strips. Numeral 99 denotes a conical, point-type horn having its throat orifice positioned at the focal point 98 and connected by the dielectric guide 100 to a translation device 101.

In the operation of the system of Fig. 5, assuming the device 101 is a transmitter, energy is supplied by the transmitter 101 over guide 100 to the horn 99 and a wave having a vertical polarization 21 (electric vector) and a spherical wave front, is propagated towards the lens 70. The phases of the wavelets passing through the thick central or vertex portion of the lens are retarded a greater amount than the phases of the wavelets propagated through the outer thinner lens portion, and the wavelets arriving at the flat front face 95 are rendered cophasal. Stated differently, the outgoing spherical wave front is converted by the lens 70 to a plane wave front extending perpendicularly to the axis 97. In reception, the converse operation is obtained, 35 and an incoming plane wave front having a propagation direction parallel to the axis 97 is transformed by the positive plano-convex lens 70 into a spherical wave front converging on the focus 98. Inasmuch as the lens 70 is circularly symmetrical, focussing action is obtained in all planes containing the axis 97.

with the invention to serve as the equivalent of a series inductance either in a
hollow pipe wave guide or in free space.
The element 34 may be made of sheet
metal of any desired thickness or it may
be made of metal foil, in which case it
may be stiff enough to be self-supporting
or it may be thin enough to require
external support. In either case it should
be thick enough substantially to prevent
penetration of the wave from one surface
of the foil to the other.

Fig. 9 shows a channel-like conductive

element which may be used in accordance

Fig. 10 shows the element 34 embedded in a filling 35 of dielectric material, e.g.; polystyrene foam, inside a section of 60 rectangular hollow pipe wave guide 36. Mounting flanges 37, 38 are shown for use in inserting the section 36 in a system of similar wave guides, either loaded or unloaded. Section 36 is thus inductively loaded and is filled, in effect, with

an artificial inductive or magnetic medium comprising the channel element 34 and the polystyrene foam 35, the latter being shown partly cut away in the figure, Internal wave reflections at the 70 walls of the wave guide 36 serve to produce in effect a magnetic medium of infinite extent filling all space. The structure of Fig. 10 has been found to be substantially the equivalent of that of Fig. 75

Fig. 11 shows a two-dimensional array of elements 34 in free space surrounded by a frame 39 and each element 34 having a supporting rectangular core 40 of 80 polystyrene foam which is in turn supported by the frame 39. The element 34 in this case may be of thin metal foil which requires external support such as is given by the foam material. The array 85 of metallic channels acts for free space waves as the equivalent of a single series inductance just as a single channel element in an enclosed wave guide acts as a single series inductive element for 90 waves confined within the wave guide. The shape of the channel element may be varied somewhat and may be U-shaped or V-shaped, for example.

Fig. 12 shows a V-shaped channel 95 member 41 which performs substantially

the same function as the member 34. Fig. 13 shows a three-dimensional array of V-shaped members 41 supported by circular slabs 42 of polystyrene foam, 100 the combination approximately filling the space of and conforming to the shape of a plano-convex lens. The lens is the substantial equivalent of one which might be made from a material having a 105 permeability materially different from that of air or free space, an example of such being a material known by the trade name of "ferroxcube" and having a permeability greater than unity for electro- 110 magnetic waves. The velocity of propagation of the waves in a permeable medium depends upon the relation

$$\frac{\mathbf{v_o}}{\mathbf{v_l}} = \sqrt{\mathcal{A}_r \, \mathbf{t_r}} \tag{9}$$

where v_0 is the velocity of waves in free 115 space, v_1 is the velocity of waves in the permeable medium, μ_r the relative permeability of the medium and ε_r the relative dielectric constant of the medium. Equation (9) indicates that a medium 120 with effective permeability greater than unity will slow down electromagnetic waves and it follows that a convex lens made of the permeable medium will cause a focussing of such waves. A lens built as 12^r shown in Fig. 13 was tested by means of

electromagnetic microwaves and found to perform as expected, that is, in a manner similar in its focussing effect to an artificial dielectric lens built as shown in Figs. 5 to 8 inclusive, and described in our copending Application Serial No. 664,672. The slabs 42 in the structure shown in Fig. 13 may be fastened together by any suitable means, e.g., with acetate cement, adhesive tape, etc.

Fig. 14 shows another plano-convex lens for electromagnetic waves, in this case comprising a combination medium having both artificial permeability and artificial dielectric constant. As in the structure shown in Fig. 13, the structure of Fig. 14 is built up from circular slabs of polystyrene foam in which are

ded V-shaped conductive elements addition, each slab has attached to f its flat surfaces a plurality of J. I conductive strips 43 which impart the designed dielectric constant to the composite artes al medium. The slabs 42 are fastened to ther in the approximate geometrical ton of a lens and may be attached to a standard or back plate 44 of polystyrene foam which in turn may be supported by an insulating base plate 45. The V-shaped elements 41 impart the artificial magnetic effect the same as in the structure of Fig. 13, it being possible to secure equivalent effects whether the points of the V's are oriented toward the planar face of the lens as in Fig. 13 or toward the convex face as in Fig. 14.

A lens constructed as in Fig. 14 has been found to focus electromagnetic waves in the expected manner and whereas either medium (dielectric or magnetic) by itself would produce strong reflections from the surfaces of the respective lens, the combination shown in Fig. 14 was found to operate with only negligible reflections from the surfaces. Figs. 15 and 16 show a converging lens of the phase-acceleration type designed for use with certain modes of transmission. The lens is composed of an array of channel members 110 or other corrugated structure alternating with smooth plates 111. The members 110 and plates 111 are supported in any suitable manner, as by rings 112 and 113 and form an artificial transmission medium. The volume of space occupied by the medium is in the shape and form of a double-concave lens. On account of the fact that this structure accelerates the phase of a wave entering it, the properties of a concave lens in this medium are ke those of a convex lens made of a dium in which the phase of a wave is ¹ed.

structure of Figs. 15 and 16 is

operative particularly with waves in which the modes of transmission are of higher order than the simplest fundamental or dominant waves.

Such of the structures shown which do 70 not depend for their operation upon properties peculiar to electromagnetic waves as distinguished from pressional waves may be used with either type of wave. Only the structure of Fig. 75 2 is in fact not adaptable to strictly analogous use with either wave type. It is to be understood, of course, that a structure for use with compressional waves requires the necessary 80 mechanical rigidity to reflect commechanical rigidity to reflect com-pressional waves from its surfaces and has no need of electrical conductivity, whereas the same or any other structure for use with electromagnetic waves 85 requires the necessary surface conductivity and requires mechanical rigidity. only to the extent that its parts be maintained in the desired positions relatively one to another. It is known of course, that 90 some modes of transmission which are possible in the case of compressional waves are not possible in the case of electromagnetic waves, and vice versa for some other modes of transmission.

It is to be noted, moreover, that at the resonant frequencies of any structure, standing waves appear instead of travelling waves and absorption of energy and filtering action occurs. It is also possible 100 at some frequencies to propagate waves in more than one mode either alone or simultaneously, which wave appearing depending in some instances upon the direction from which the resonant fre- 105 quency is approached as the frequency is varied in the neighbourhood of the resonant frequency.

What we claim is:-1. A device for changing the velocity 110 of propagation of waves of radiant energy, comprising a plurality of recessed elements positioned within a bounded region of a medium of a given characteristic impedance, each said ele-115 ment being composed of a material having a characteristic impedance for said waves that is of a different order of magnitude from that of said medium, said elements being separated from each 120 other by portions of said medium, which portions are interconnected for the transmission of said waves through said bounded region, said plurality of elements being distributed over an area 125 transverse to the direction of propagation of said waves.

2. A device according to claim 1, in which the boundaries of said bounded region are of the shape of an optical re- 130

given a desired value. characteristic impedance of the device is 3, in which the recessed elements are interspersed with flat strip elements of said region are of the shape of an optical lens which the boundaries of said bounded A device according to claim 1, 2 or so that the resultant effective

arranged in a spaced parallel array, o impedance for said waves, comprising a parallel plurality of strip elements in a spaced of propagation of waves of radiant energy array of said strip elements being interin a medium of a given characteristic array, a Ŷ. channel-shaped two-dimensional subelements

sional subarrays of channel-shaped elements, said channel-shaped elements of said medium. a different order of magnitude from that tic impedance for said waves that is of and said strip elements each being composed between two adjacent two-dimenposed of a material having a characteris-

elements each comprise a channel-shaped A device according to any of the preceding claims, in which said recessed

the frequency of a wave to be refracted. are resonant at a frequency higher than 7. A device according to any of the preceding claims, in which said elements

elements are formed is conductive. 8. A device according to any of the preceding claims, for free space plane polarized 9. A device according to any of the electromagnetic materia which waves, said

which said elements are mounted solid dielectric medium. waves, in which said elements are rigid. preceding 10. A device according to claim 8, in claims, compressional

prises polystyrene foam.

12. A lens for electromagnetic waves, comprising a plurality of circular clara which said solid dielectric medium com-11. A device according to claim 10, in

A device according to claim 2, it a desired artificial dielectric constant. faces of each dielectric slab to impart to LO. A lens according toyclaim 12; in-cluding also a plurality of spaced conducing to the shape of a plangeonyew 13. A lens according togethim ! mately filling the space of and contorm-14. A lens according to claim 12 or 13,

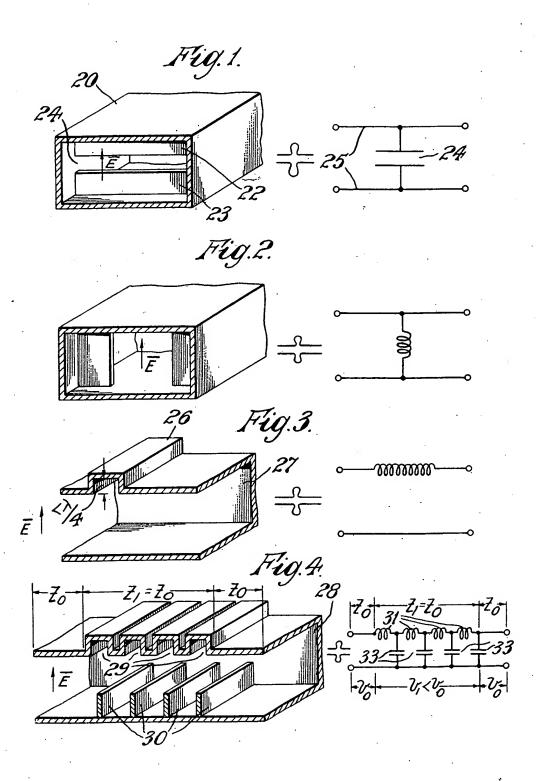
5. A device for changing the velocity in which said recessed elements are

substantial fraction of the design wavecesses in said elements have depths a of the preceding claims, in which the relength and materially less than 15. A device or a lens according to any

and constituting shunt capacitive eleother portion of the wall of said guide ments at the said operating frequency. of partial barrier plater attached to anfrequency of said system i sid a plurality series inductive elements such operating dielectric wave guide and recesses in a portion of the wallplurality of cavity resonators for plurality of cavity resonators 16. A wave guide, system compr

guide. citive members while making the velocity different from that in the of said series inductive and shunt capa- 95 wave guide as unmodified by the presence characteristic impedance of the system substantially identical with the characseries inductance and shunt capacitance teristic impedance of the said dielectric are so proportioned as to make the 17. A wave guide system according to claim 16, in which the effective values of propagation of waves

operate substantially as herein described drawings. shown in Fig. 4 of the accompanying herein described with reference to and as and adapted to operate substantially as 19. A lens constructed and adapted to10 18. A wave guide system constructed



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SHEETS 1 & 2

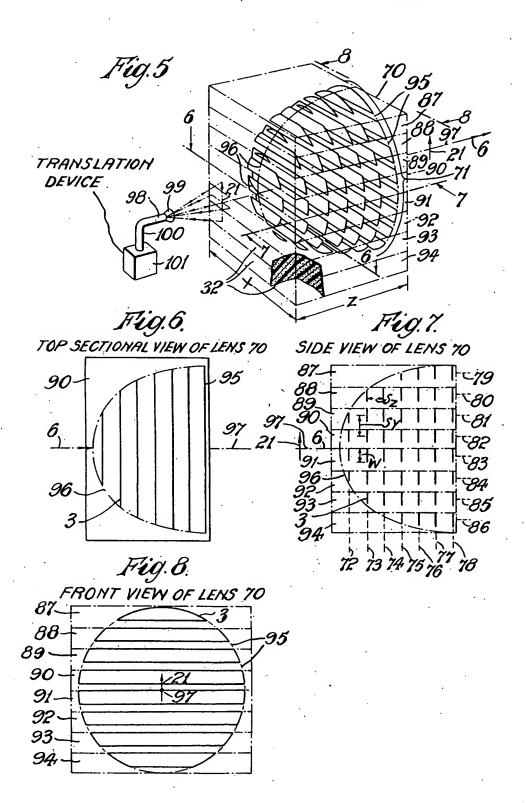


Fig. 10. Fig.11. 40 Fig. 13. 43=

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SHEETS 3 & 4

Fig. 15

